Research paper

Gas hydrate quantification at a pockmark offshore Norway from joint effective medium modelling of resistivity and seismic velocity

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ABSTRACT

Methane emissions from gas hydrate deposits along continental margins may alter the biogeophysical properties of marine environments, both on local and regional scales. The saturation of a gas hydrate deposit is commonly calculated using the elastic or electrical properties measured remotely or in-situ at the site of interest. Here, we used a combination of controlled-source electromagnetic (CSEM), seismic and sediment core data obtained in the Nyegga region, offshore Norway, in a joint elastic-electrical approach to quantify marine gas hydrates found within the CNE03 pockmark. Multiscale analysis of two sediment cores reveals significant differences between the CNE03 pockmark and a reference site located approximately 150 m northwest of CNE03. Gas hydrates and chemosynthetic bivalves were observed in the CNE03 sediments collected. The seismic velocity and electrical resistivity measured in the CNE03 sediment core are consistent with the P-wave velocity ($V_P$) and resistivity values derived from seismic and CSEM remote sensing datasets, respectively. The $V_P$ gradually increases (~1.75–1.9 km/s) with depth within the CNE03 pipe-like structure, whereas the resistivity anomaly remains ~3 $\Omega$m. A joint interpretation of the collocated seismic and CSEM data using a joint elastic-electrical effective medium model suggests that for the porosity range 0.55–0.65, the gas hydrate saturation within the CNE03 hydrate stability zone varies with depth between ~20 and 48%. At 0.6 porosity, the hydrate saturation within CNE03 varies between ~23 and 37%, whereas the weighted mean saturation is ~30%. Our results demonstrate that a well-constrained gas hydrate quantification can be accomplished by coupling P-wave velocity and CSEM resistivity data through joint elastic-electrical effective medium modelling. The approach applied in this study can be used as a framework to quantify hydrate in various marine sediments.

1. Introduction

Hydrate-bearing sediments at continental margins and permafrost regions contain methane volumes comparable to global fossil fuel reserves (Collett, 2002; Milkov and Sassen, 2002; Milkov, 2004; Klauda and Sandler, 2005; Pinero et al., 2013; Boswell et al., 2015). The environmental and economic implications of methane lead to a growing need for efficient and reliable methods for gas hydrate deposits quantification (Collett et al., 2009; Ruppel, 2011; Boswell et al., 2014; Marin-Moreno et al., 2015; Collett and Boswell, 2012; Li et al., 2016). Direct and accurate quantification of gas hydrate using pressure core sampling may lead to equivocal interpretations, due to uncontrolled core recovery-induced hydrate dissociation, gas expansion, and exsolution effects (e.g., Milkov et al., 2004; Holland et al., 2008; Collett et al., 2008). Sonic velocity and electrical resistivity data obtained from well-log measurements are conventionally used to estimate hydrate saturation (e.g., Pearson et al., 1983; Hyndman et al., 1999; Collett and Ladd, 2006; Collett and Boswell, 2012). However, well-log operations are technically complex, expensive, and only provide localized information (Collett et al., 1998; Hyndman et al., 1999; Collett and Ladd, 2006; Riedel et al., 2006). Gas hydrate saturations within a single reservoir unit could vary significantly (e.g., Torres et al., 2008;
Malinverno et al., 2008; Riedel et al., 2009); thus, localized pressure cores and well-log measurements may not adequately represent large-scale hydrate reservoirs.

In contrast, remote sensing methods such as marine controlled-source electromagnetic (CSEM) and seismic surveys provide regional data, enable larger scale detection, delineation and potential quantification of gas hydrate deposits (e.g., Singh et al., 1993; Wood et al., 2000; Lodolo et al., 2002; Lee et al., 2005; Weitemeyer et al., 2006; Schwalenberg et al., 2010; Attias et al., 2016). Coincident well-log data can calibrate the data acquired using these remote sensing techniques. Electrical resistivity measured by CSEM provides information about the pore fluids properties and distribution, complementary to structural information obtained from seismic data. Thus, a joint interpretation of coincident seismic and CSEM data enhance the characterisation of gas hydrate deposits (Attias et al., 2016; Goswami et al., 2017; Schwalenberg et al., 2017). However, such joint elastic-electrical approaches require a suitable rock physics framework to constrain the elastic-electrical parameters and link them to petrophysical properties of the reservoir (e.g., Du and MacGregor, 2016).

The elastic and electrical properties of sediments are predominantly controlled by parameters such as mineralogy, porosity, pore-fluid and saturation, grain shape/alignment, and temperature (e.g., Ellis et al., 2010). In order to fully exploit the elastic and electrical properties of rocks, both property responses should be linked by a common microstructure. Effective medium methodologies can be used to derive the joint bulk elastic and electrical properties of microheterogeneous sedimentary rocks (e.g., Sheng, 1990, 1991; Berryman, 1992; Hornby et al., 1994; Carrara et al., 1994; Jakobsen et al., 2000; Carcione et al., 2007). In this study, “microheterogeneous” refer to different constituents composite and their configurations, as explained in section 5.1. The effective medium models are based on first-principle physics, where the effective properties of a composite are derived from the properties of its individual constituents (e.g., quartz, clay, calcite, etc.)
and their arrangements, giving an idea of the topology of the medium.

In this work we employ an effective modelling scheme based on a combination of the self-consistent approximation (SCA) (e.g., Hill, 1965; Te Wu, 1966) and the differential effective medium (DEM) (e.g., Cleary et al., 1980; Berryman, 1992) theories. A detailed motivation for this approach is given by Sheng (1990), who was the first to introduce this concept. Sheng (1990) showed that the combined SCA/DEM method reproduces the microstructural feature of biconstancy of phases in sedimentary rocks at any finite porosity, which implies the existence of fluid pathways. This approach has been used with success in modelling bulk elastic properties of shales (e.g., Hornby et al., 1994), hydrate-bearing sediments (e.g., Jacobsen et al., 2000; Chand et al., 2006; Ghosh et al., 2010), and the joint elastic-electrical properties of clay-bearing sandstones (e.g., Han et al., 2011a).

Although effective medium theories have been used for modelling the elastic properties of hydrate-bearing sediments, a joint elastic-electrical effective medium modelling approach has not been applied for hydrate estimation, to the best of our knowledge. Here, we model the joint elastic-electrical properties of clay-rich, hydrate-bearing sediments by extending the modelling approach of Han et al. (2011a). Detailed analysis of sediment cores from a gas hydrate pipe-like structure and an adjacent reference site provided us with (i) physical evidence for the existence of gas hydrate at the site of interest, (ii) localised porosity, elastic, and electrical properties, and (iii) characterisation of the lithology in three different length scales: macro, meso, and micro. We used the information obtained from these cores for the model inputs and to confirm the background sediment resistivity and velocity values (from seismic and CSEM data) used for calibration of the effective medium model. This approach helped us to constrain many of the model input parameters. The resulting joint elastic-electrical effective medium model was then applied for hydrate quantification using seismic and CSEM datasets from our study region, which were previously analysed by Plaza-Faverola et al. (2010) and Attias et al. (2016), respectively.

We note that for our study region, there is evidence suggesting that the gas hydrate forms in pore-filling, fracture-filling, or a combination of both (e.g., Westbrook et al., 2008a; Plaza-Faverola et al., 2010). For fracture-filling hydrate, a rigorous effective medium modelling is beyond the scope of this paper. However, because limited electrical anisotropy detected by CSEM inversions at the site of interest (Attias et al., 2016) precludes the presence of hydrate in strongly aligned fractures, we can make the following approximation: If fractures are randomly oriented and we are averaging over large volumes, then the fracture-filling can be treated as pore-filling (with the fractures being the pores) but with a lower aspect ratio (i.e. effective medium). For pore-filling hydrate, we take the analysis further by applying a fully rigorous effective medium modelling scheme (sections 5.1, 5.2, and 6.2–6.4).

Our case study focuses on the CNE03 pockmark (Fig. 1). This pockmark has a Type-2 morphology, according to the classification system of Sultan et al. (2010); Riboullet et al. (2011, 2016). A Type-2 pockmark is defined as complex seafloor morphology underlain by irregular pipe-like structure, which is primarily controlled by the formation and decomposition of gas hydrate. The CNE03 pockmark is underlain by an irregular pipe-like structure that is ~200 m in diameter at the seabed and ~500 m at the base of the gas hydrate stability zone (BGHSZ) (e.g., Bünz et al., 2003; Plaza-Faverola et al., 2010).

2. Geologic setting

The Norwegian Marginal Sea is located northwest of Norway, bound by the North and Greenland Seas between 62°N, 5°E to 71°N, 25°E (Eastern flank); and 62°N, 6°W to 65°N, 13°W (Western flank). The Norwegian continental margin encompasses the Nyegga region (Fig. 1, inset map), which is positioned NW of the Storegga slide between the Voring and Møre sedimentary basins, extending over 200 km² (e.g., Bünz et al., 2003; Brekke, 2000). The Nyegga region lies in water depths of ~700–800 m, with a seafloor slope angle of ~1° (Hovland et al., 2005; Plaza-Faverola et al., 2010). Both the Nyegga and Storegga regions show sediment compaction patterns with varying thicknesses, resulting from glacial-interglacial climate cycles (e.g., Dahlgren et al., 2002; Kjeldstad et al., 2003). The Miocene/Early Pliocene Kai and the Plio/Pleistocene Naust sediment formations (e.g., Dalland et al., 1988; Eidvin et al., 1998) host the Nyegga and Storegga gas hydrate systems (e.g., Bünz et al., 2003; Berndt et al., 2003; Westbrook et al., 2008a; Senger et al., 2010). The Kai Formation sediment consists of fine-grained hemipelagic oozes, whereas the Naust Formation is characterised by sharp lithological fluctuations resulting in debris flow deposits and hemipelagic sediments (Bünz et al., 2003; Hustoft et al., 2007).

Elongated northwards, approximately 240 km long and 60 km wide, the Helland–Hansen Arch anticline lies beneath Nyegga (e.g., Kjeldstad et al., 2003). This anticline has enabled upwards thermogenic gas propagation from deep hydrocarbon-rich reservoirs, promoting fluid expulsion which disrupted the seabed homogeneity by forming an extensive pockmark field along the Nyegga region (Judd and Hovland, 1992; Bouriak et al., 2000; Hovland et al., 2005; Hovland and Svensen, 2006; Plaza-Faverola et al., 2010). These pockmarks are underlain by pipe-like structures, caused by the vertical movement of fluids and gas (e.g., Bouriak et al., 2000; Berndt et al., 2003; Plaza-Faverola et al., 2011). Nyegga's pipe-like structures accommodate gas hydrates in a low saturation state, with an estimated total volume of 710 GSm³ (GSm³ = 10⁹ standard cubic metres) over the Nyegga area, which is equivalent to ~4500 million barrels of oil (Senger et al., 2010). One of Nyegga's pipe-like structures is the CNE03 pockmark, which is thought to contain moderate-to-high concentration of hydrates that either forms in sub-vertical veins, subsequent to vertical migration of thermogenically-sourced gas into the hydrate stability zone (Plaza-Faverola et al., 2010); or/and forms in a pore-filling morphology, particularly near the BGHSZ as previously indicated for this region (e.g., Westbrook et al., 2008a; Plaza-Faverola et al., 2010). At its centre, the CNE03 pipe-like structure presents intense seismic scattering and attenuation and is bounded by the pull-up of reflectors in its margins (Ivanov et al., 2010; Plaza-Faverola et al., 2011, 2012). The CNE03 pockmark is covered by glacial-interglacial silty clay hemipelagic sediments (e.g., Bünz et al., 2003; Ivanov et al., 2010).

3. Data and methods

3.1. Seismic and CSEM data

Seismic and CSEM surveys conducted at the CNE03 pockmark provided data for a comprehensive analysis of the elastic and electrical properties of this pockmark. In brief, Plaza-Faverola et al. (2010) constructed a P-wave velocity (Vp) model using Tomolnv, a reflection time tomography software (Delbos et al., 2001, 2006). Their model shows that the Vp within the CNE03 pipe-like structure ranges between ~1.6 and 1.9 km/s (Fig. 2a), collocated with a columnar seismic blanking zone (CSBZ) that is often associated with the presence of hydrates (e.g., Riedel et al., 2002; Boswell et al., 2015). Adjacent to the CNE03 pipe structure (200 m north of CNE03), the background velocity ranges between ~1.6 and 1.7 km/s. The velocities in the upper part of the seismic tomography model (< 1.7 km/s between 0 and 80 m below seafloor) are poorly constrained, due to low ray coverage (Plaza-Faverola et al., 2010). Within the CNE03 pipe-like structure, between 80 m below seafloor (mbsf) and 280 mbsf (BGHSZ), the Vp gradually increases. For comparison with our effective medium model, we divided this varying Vp into three depth intervals and averaged the values of each region, yielding velocities of 1.75 km/s (Vp1), 1.83 km/s (Vp2), and 1.9 km/s (Vp3) for depth intervals of 80–180, 180–200, and 200–280 mbsf, respectively (Fig. 2a).

Attias et al. (2016) delineated the resistivity structure beneath the CNE03 pipe-like hydrate accumulation (Fig. 2b) using 2.5-D CSEM
inversion constrained by the collocated seismic reflection and tomography information (Westbrook et al., 2008b; Plaza-Faverola et al., 2010, 2012). This CSEM inversion gave resistivity values of $\sim 3$ $\Omega m$ within the CNE03 pipe-like structure, and a background resistivity of $1.3–1.5$ $\Omega m$ north of CNE03, collocated with the background $V_p$ (Fig. 2). These resistivity values have been confirmed by 2.5-D CSEM inversions of a towed-receiver data (Attias et al., 2018). To be consistent with the $V_p$ data, we extracted the resistivity values observed between 80 and 280 mbsf (Fig. 2b). However, we found that the resistivity variations within this depth interval are insufficient to justify a different depth discretization as was done for the velocity model.

3.2. Sediment core data

Sediment cores were collected from within the CNE03 pockmark, and from a nearby reference site (i.e., regional background). To study the characteristics of a gas hydrate driven lithology, for Multiscale analysis, we discretized the sediment cores to three different scales - meter (Macro), centimetre (Meso) and sub-millimeter (Micro) scales.

3.2.1. Macro-scale: sediment core acquisition & petrophysical measurements

Sediment cores of $\sim 6.8$ m and $\sim 8$ m length were recovered from the CNE03 pockmark and a background site, respectively, using a piston corer. The background site is located $\sim 150$ m NW from the CNE03 pockmark (Fig. 1), and hence represents undisturbed sediments for comparison with hydrate-bearing sediments. Both sediment cores were immediately split after collection into 1.25 m length sections (15 in total) and stored at 5°C. A macro-scale analysis was performed using all sediment sections. First, the core sections were measured for petrophysical properties (P-wave velocity, electrical resistivity, gamma density, magnetic susceptibility) using the Geotek Multi-Sensor Core Logger (MSCL-S) (Weaver and Schultheiss, 1990; Weber et al., 1997). Ultrasonic $V_p$ was measured using the pulse-echo technique (McCann and Sothcott, 1992), which provides usable frequencies between 300 and 1000 kHz with absolute accuracies of $\pm 0.3$% for velocity (Best, 1992). We use here the $V_p$ values at a single frequency of 600 kHz, obtained from Fourier analysis of broadband signals.

For the electrical resistivity tomography (ERT), we measured the electrical resistivity using 16 stainless steel electrodes, distributed radially in two rings around the sample. The sixteen resistivity measurements were taken using 0.5 mA of alternating current at a frequency of 80 Hz, then averaged to yield a single resistivity value per each sample. Thirteen consecutive measurements are made with all offset electrode pairs, resulting in a total of 208 measurements. The ERT data were inverted using an isotropic finite element algorithm, to derive the resistivity
distribution from the measured voltage (North et al., 2013). The accuracy of this measurement is ± 5%, for samples with electrical resistivity range of 1–100 Ωm (North et al., 2013; North and Best, 2014). All the elastic and electrical measurements were conducted at a temperature of ~2°C, in a laboratory with a controlled ambient temperature of ~20°C and humidity of 55%. The porosity was later calculated from weight differences between the saturated and oven-dried (at 40°C) samples. The wet (macro-scale) and dry (meso-scale) porosity measurements are reasonably consistent, with comparable trends and very subtle differences that we attribute to local heterogeneities (Fig. 3b).

3.2.3. Micro-scale: X-Ray computed tomography (X-CT) scans

To analyse the background and CNE03 sediment cores on a micro-scale, we performed CT scans using a GE Phoenix industrial X-CT. CT imaging can contribute to assessing grain size, density and porosity, and detect any presence of biota (e.g., Bin et al., 2013). For this purpose, ~2 mm diameter samples from the top of each background and CNE03 core section (Fig. 3a and c) were carefully extracted and placed in X-ray scanning tubes. The samples were scanned using 80 kV and 120 μA, producing high-resolution ~4 μm X-CT images.

3.3. Micro-scale: X-ray diffraction (XRD) measurements

To characterise the mineralogy of the CNE03 sediment, we performed a series of X-ray diffraction (XRD) measurements. A semi-quantitative bulk mineral analysis from standards was undertaken using a least squares method similar to that used in FULLPAT (Chipera and Bish, 2002) and the Microsoft Excel-based programs RockJock (Eberl, 2003).

4. Results

4.1. Sediment core analysis

In general, the background core contained consistently pale brown foraminifera-rich sediment, whereas the CNE03 core exhibit a varied lithology of finely-grained ooze and coarse shell horizons (Fig. 3a and c). The background sediment represents a continuous hemipelagic sequence (Lithofacies B), containing variations in microfossils (no macrofossils observed) and lithic content consistent with slowly settled marine clays (Fig. 3a, Table 1). No hydrates or cavities were observed in the background core upon recovery (Fig. 3a).

The CNE03 sediment varies from pale grey to green-grey, with sparse cavities (Fig. 3c). During onboard core segmentation, visual observation revealed chunks (~2 cm in length) of hydrates at the base of the CNE03 core (Figs. 1 and 3c), which decomposed via bubbling, similar to the dissociation of near-seabed hydrate accumulations recovered from within the CNE03 pockmark by Ivanov et al. (2007). Two
shell horizons are observed within the CNE03 core (Fig. 4), hosting sporadic dark grey carbonate nodules. These horizons are marked by a gradual increase of the shell frequency, best observed in the X-ray images (Fig. 4b). The extracted shell (Fig. 4c and d) was identified as the chemosynthetic *Isorropodon nyeggaensis* sp. bivalve (Krylova et al., 2011), also referred to as *Catypogena* sp. (Ivanov et al., 2010). The *Isorropodon nyeggaensis* sp. bivalve belongs to the chemosymbiotic families, which metabolise organic substance via chemosymbiosis by hosting intracellular sulfide-oxidising bacteria (e.g., Cavanaugh, 1983; Distel, 1998). The *Isorropodon nyeggaensis* bivalves were previously utilised as a model-dependent time marker for methane seepage in the Nyegga pockmark field, where sediment cores from a seep-related structure detected a 60 cm layer of *Isorropodon nyeggaensis* shells at 100 cm depth (Karstens et al., 2018). Thus, *Isorropodon nyeggaensis* sp. shell fragments retrieved from the CNE03 cores provides additional evidence for contemporary methane influx and subsequent hydrate formation within the CNE03 pipe-like structure.

The CNE03 core macro-scale measurements present a higher $V_p$ and resistivity values than the background core, whereas the porosity in both cores ranges between $\sim$0.55 and $\sim$0.65 (Fig. 3b). The CNE03 $V_p$ macro-scale measurement is abrupt, segmented, and only extends to $\sim$2.2 mbsf (Fig. 3b). The high $V_p$ observed in the CNE03 core between $\sim$1.5–2.2 mbsf is attributed to a shell horizon, whereas below $\sim$2.2 mbsf no $V_p$ measurement was obtained, most likely due to the presence of cavities (i.e., low-density), as shown in Fig. 3c. The higher macro-scale resistivity measurement of the CNE03 core in comparison to the background core (Fig. 3b), is attributed to the freshening of pore water during hydrate dissociation on core recovery. The macro-scale resistivity measurement of the background core is comparable with a resistivity log obtained from a borehole located $\sim$24 km NW of the CNE03 pockmark (Senger et al., 2010). The background sediments are less disrupted than the CNE03 sediments, as indicated by the core images (Fig. 3a and c). We note that the macro-scale $V_p$ and resistivity values derived from both the background and CNE03 cores are comparable to the remotely-sensed $V_p$ and CSEM resistivity values (Figs. 2 and 3).

The average porosity calculated from both the background and CNE03 macro-scale measurements is approximately 0.6 (Fig. 3b), consistent with a nearby well-log data (Hustoft et al., 2009). The Image of section A of the CNE03 core (Fig. 3c), shows two cavities that are attributed to the dissociation of pre-existing hydrate because at core recovery, gas hydrates occupied (Fig. 1) the cavity observed at $\sim$6.8 mbsf (Fig. 3c). In spite of these apparent cavities, the macro-scale porosity measurements obtained from the background and CNE03 sediment cores are comparable (Fig. 3b and c). The comparison of the two sediment cores demonstrates the distinct difference between undisturbed regional sediments and profoundly disturbed sediments beneath the CNE03 pockmark, that we attribute to methane flux into the GHZ, the resulting hydrate formation process, and the presence of shells.

### 4.2. Electrical resistivity tomography

Fig. 5 shows a comparison between the ERT of the background and CNE03 meso-scale samples, as retrieved from $\sim$6.8 mbsf. ERT of the background sample yields a relatively low and homogenous resistivity (Fig. 5a) compared to the heterogeneous and higher resistivity observed in the CNE03 sample (Fig. 5b). The resistivity of the background sample ($\sim$2–3 $\Omega$m) is consistent with the resistivity obtained from the macro-scale measurement (Fig. 3b). The relatively high resistivity ($\sim$3–6 $\Omega$m) observed in the CNE03 sample might be related to pore-water freshening from hydrate dissociation, or the presence of electrically resistive shells (Fig. 3b and c, and 4), but most likely a combination of these two factors. This meso-scale ERT analysis supports the notion that the CNE03 core sample previously contained hydrates, which dissociated during core recovery.

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**Table 1** Main lithofacies units of the background and CNE03 sediment cores.

<table>
<thead>
<tr>
<th>Units</th>
<th>Description</th>
<th>Boundaries</th>
<th>Interpretation</th>
</tr>
</thead>
<tbody>
<tr>
<td>BG1</td>
<td>Winnowed Holocene sands</td>
<td>Indistinct, non-erosive</td>
<td>None visible, grades into lithofacies D</td>
</tr>
<tr>
<td>BG2–BG10</td>
<td>Hemipelagic diamicton</td>
<td>None visible, grades into lithofacies D</td>
<td>Diffuse, concentration of shells gradually increases and decreases within surrounding sediments</td>
</tr>
<tr>
<td>CN1</td>
<td>Altered hemipelagic and pockmark ooze</td>
<td>Undulating lower boundary, upper surface at core top</td>
<td>Presence of chemosynthetic shells due to free gas fluxes and hydrate formation</td>
</tr>
<tr>
<td>CN3, CN5</td>
<td>Altered hemipelagic and pockmark ooze</td>
<td>Indistinct, non-erosive</td>
<td>Presence of chemosynthetic shells due to free gas fluxes and hydrate formation</td>
</tr>
<tr>
<td>CN1, CN3, CN5</td>
<td>Altered hemipelagic and pockmark ooze</td>
<td>Indistinct, non-erosive</td>
<td>Presence of chemosynthetic shells due to free gas fluxes and hydrate formation</td>
</tr>
<tr>
<td>CN2, CN4</td>
<td>Altered hemipelagic and pockmark ooze</td>
<td>None visible, grades into lithofacies D</td>
<td>Diffuse, concentration of shells gradually increases and decreases within surrounding sediments</td>
</tr>
<tr>
<td>D</td>
<td>Shell horizon of intact chemosynthetic Isorropodon bivalve</td>
<td>Indistinct, non-erosive</td>
<td>Presence of chemosynthetic shells due to free gas fluxes and hydrate formation</td>
</tr>
</tbody>
</table>

*a* BG units = Background sediment, CN units = CNE03 sediment.

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*Note:* The resistivity log obtained from a borehole located $\sim$24 km NW of the CNE03 pockmark field was previously utilised as a model-dependent time marker for methane seepage in the Nyegga pockmark field, where sediment cores from a seep-related structure detected a 60 cm layer of *Isorropodon nyeggaensis* shells at 100 cm depth (Karstens et al., 2018). Thus, *Isorropodon nyeggaensis* sp. shell fragments retrieved from the CNE03 cores provides additional evidence for contemporary methane influx and subsequent hydrate formation within the CNE03 pipe-like structure.

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4.3. X-ray computed tomography

The X-CT scans illustrate the microstructure of the sediments obtained from the background and CNE03 micro-scale samples (Fig. 6). The background sample is relatively homogeneous, finely-grained and tightly compacted (Fig. 6a). The CNE03 sample is heterogeneous, and contain finely-grained oozes and coarse shell horizons (Fig. 6b). The CNE03 micro-scale sample shows a wide range of pore volumes (Fig. 6c), presumably caused by the dissociation of pre-existing hydrates.
4.4. X-ray diffraction analysis

Our XRD analysis indicates that the dominant mineralogy in the core samples is clay, making up 55% of the sediment composition, followed by 17.5% quartz and smaller concentrations of calcite, magnesium calcite and K-feldspar (Table 2).

5. Data assessment using effective medium modelling

5.1. Effective medium modelling approach

Effective medium theories have been used widely and successfully to model the bulk response of a microheterogeneous composite (e.g., Sheng, 1990; Ellis, 2008; Han et al., 2011a). Although effective medium theories do not incorporate the actual description of the microstructure, one can still deduce it as these theories do have physical representations of the involved elements (Jakobsen et al., 2000). The microstructural features of a composite medium control its elastic and electrical properties to a large extent, and as such, a consistent description of the seismic and electrical response of a medium should incorporate some detail of the microstructural configuration.

Pore-filling and grain-displacing are the most common gas hydrate morphologies observed in marine environments (e.g., Riedel et al., 2006; Collett et al., 2008; Boswell et al., 2009). At depth, under high-pressure and low-temperature conditions, it is feasible that hydrate forms as pore-filling within the pore space between sediment grains (Dai et al., 2012). A two-phase (hydrate and fluid) numerical model by Nimblett and Ruppel (2003) suggests that with increasing depth, hydrate forms more homogeneously in a pore-filling morphology than in fractures, which is consistent with our remotely-sensed $V_p$ and resistivity models of CNE03 (Fig. 2). Ivanov et al. (2007) analysis of core samples collected from the CNE03 pockmark indicate that hydrate forms in both pore-filling and grain-displacing morphologies. Hydrate can be distributed in grain-displacing morphology in various ways (e.g., Jakobsen et al., 2000; Ghosh et al., 2010; Best et al., 2013). Using elastic properties in a combined self-consistent approximation (SCA) and differential effective medium (DEM) model, Ghosh et al. (2010) demonstrated that a pore-filling morphology only moderately alters the inferred hydrate saturation in comparison to a mixture of pore-filling and grain-displacing morphology. Thus, although grain-displacing morphology may also be present at depth in CNE03, here, we applied the case of a pore-filling morphology for our SCA/DEM model to estimate the hydrate saturation within the deeper zone of the CNE03 pockmark.

The elastic and electrical properties of rocks and sediments are significantly affected by their microstructure. Therefore, the modelling should consider differences in the microstructural distribution of the rock constituents. In practice, collocated measurements of elastic and electrical properties are derived from a single microstructure; hence, capturing this consistency is essential for a rigorous rock physics approach. The SCA and DEM theories (and the combination of both) used in this study have elastic and electrical formulations with a consistent microstructural description between both properties.

Sedimentary rocks generally contain phases that are bicontinuous (i.e., the pore space is connected, and the solid phase is also continuous) at any finite porosity (e.g., Berryman, 1992; Hornby et al., 1994). The model considered here is a bicontinuous sediment and pore space, where

Table 2

<table>
<thead>
<tr>
<th>Mineral</th>
<th>Quantity (per cent)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clay</td>
<td>55</td>
</tr>
<tr>
<td>Quartz</td>
<td>17.5</td>
</tr>
<tr>
<td>Calcite</td>
<td>8</td>
</tr>
<tr>
<td>Magnesium Calcite</td>
<td>8.2</td>
</tr>
<tr>
<td>K-feldspar</td>
<td>3.6</td>
</tr>
</tbody>
</table>

* The sediment sample for XRD was obtained from the CNE03 core at ~6 mbsf.

* Magnesium Calcite is indicative of biogenic activity.
the pore space contains hydrate and brine connected phases. In effect, we have a three-phase composite consisting of connected sediments, hydrate, and brine. Limited observations available on hydrate morphology in sediments suggests that hydrate connectivity increases with the degree of hydrate saturation (e.g., Chaouachi et al., 2015). The use of a connected hydrate framework is appropriate for the CNE03 pockmark, because previous studies infer a moderate-to-high saturation (23–45%) of hydrates at CNE03 (e.g., Westbrook et al., 2008b; Plaza-Faverola et al., 2010).

Sheng (1990) introduced an approach for creating a biconnected two-phase composite by combining the SCA and DEM theories. The DEM theory ensures the connectivity of the background phase (the starting phase), while the inclusions remain isolated at any given porosity (e.g., Berryman, 1992; Hornby et al., 1994). However, the SCA theory implies a biconnected effective microstructure between porosities of 0.4 and 0.6 (Sheng, 1990; Jakobsen et al., 2000). We refer to the porosities where the phases are connected in the SCA theory as the critical porosity ($\phi_c$) (e.g., Ellis, 2008; Han et al., 2011a). This biconnectivity of phases might not be very important for modelling some properties, as it has been used successfully, for example, to model elastic properties (Sheng, 1990). Nevertheless, using the same approach for elastic DEM and electrical DEM of sandstone would grossly overestimate the electrical resistivity, well beyond what is seen in practice (e.g., Han et al., 2011a). Therefore, neither the SCA nor DEM theories can model independently the effective properties of a biconnected composite at any porosity, making a combination of both theories essential.

In this study, we have adopted the approach used by Han et al. (2011a). Although Han et al. (2011a) modelled sandstones, the approach is not specific to sandstones as the effective medium models are not specific to any composite, one of the reasons why these models are attractive (Sen et al., 1981; Milton, 1985; Berryman and Hoversten, 2013). Here, we used the effective medium models for clay-rich sediments (e.g., Hornby et al., 1994). The SCA and DEM equations used here (Appendix A) are isotropic formulations (e.g., Mavko et al., 1998; Ellis, 2008; Han et al., 2011a). For a two-phase (e.g., sediment and brine) medium (e.g., Sheng, 1990; Jakobsen et al., 2000; Han et al., 2011a), the procedure for creating a biconnected composite is as follows: First, we obtain an effective medium at the $\phi_c$ (i.e., a porosity where the phases are biconnected, e.g., 0.4, 0.5, or 0.6) using the SCA theory; second, the DEM theory is used to obtain the effective medium at any porosity by starting with $\phi_c$ value as the background; finally, sediments are added for porosities $<\phi_c$ and brine for porosities $>\phi_c$, as illustrated in Fig. 7a. This gives the effective properties of a biconnected composite at any porosity. We model the hydrate-bearing sediments as a three-phase fully connected system that is composed of sediments, brine and hydrates. The mineral content of the sediments is known from the XRD analysis (section 4.4). We used the XRD information to construct a single mineral phase labeled as CQ mix, a sediment composition that encompasses two primary minerals (clay, quartz) and three residual minerals (calcite, magnesium calcite, K-feldspar). For modelling simplification, the three residual minerals were added to the quartz content. Thus, the CQ mix contains 55% of clay and 45% of quartz minerals (Table 2).

We obtain a three-phase effective medium by repeating the two-phase modelling (CQ mix), with the sequence determining the microstructural representation of the final medium (Han et al., 2011a). For a brine saturated, clay-rich sediment with pore-filling hydrates, where all the constituents are connected, the procedure is as follows: First, we use the two-phase SCA/DEM method to combine the hydrate and brine; then, we combine this hydrate + brine mix with the CQ mix using the two-phase SCA/DEM approach again, giving the final three-phase effective medium (Fig. 7).

### 5.2. Joint elastic-electrical SCA/DEM application to seismic & CSEM data from CNE03

We apply the effective medium modelling approach described above to estimate the hydrate content from the velocity and resistivity values as obtained from the seismic and CSEM datasets, respectively (section 3.1). The depth of interest ranged between 80 and 280 mbsf, where both velocity and resistivity anomalies are observed within CNE03 pipe-like structure are robust (Fig. 2), coincident with gas hydrate driven CSBZ. Ideally, one would calibrate the effective medium model from controlled laboratory experiments on hydrate-bearing sediments obtained from the site of interest. In the absence of such measurements, alternatively, we can use data from an undisturbed reference site, and thus, unbiased by free gas influx and hydrate formation/dissociation effects, or other local heterogeneities. Therefore, we have adopted the following approach: First, we fit a two-phase SCA/DEM model of sediments (CQ mix) and brine to the remotely-sensed data background response (no hydrate) by seeking a realistic combination of inputs. This step is done to calibrate some input model parameters in order to obtain a base model. Second, we apply the calibrated model parameters to obtain the three-phase effective medium modelling, as described in section 5.1.

The inputs for individual constituents in effective medium models are (i) the bulk and shear moduli for the elastic models, (ii) the electrical resistivity for the electrical models, and (iii) the aspect ratios and volume fractions for both models. Although the bulk and shear moduli of clay minerals are poorly known because of the absence of large crystals for direct measurements, there is a reasonably narrow range that is widely used in the literature (e.g., Hornby et al., 1994; Jakobsen et al., 2000; Ellis, 2008; Han et al., 2011a). Likewise, electrical resistivity values of clay minerals are not well known, unlike quartz and carbonates which are usually taken as insulators. However, values that fall within the range of 1–100 $\Omega$m are reported (e.g., Telford et al., 1990; Han et al., 2011a). For the initial two-phase background model, we assumed a pore-fluid salinity range of 60–40 ppt (Smith et al., 2014) for background sediments between 80 and 280 mbsf, respectively. These salinity values are equivalent to resistivity range of 0.16–0.19 $\Omega$m, by applying the equations of state proposed by Pofonoff (1985); Lewis and Perkin (1981).

The values given in Table 3 were used to calibrate the two-phase SCA/DEM model to the averaged values of the background velocity (1.7 km/s) and resistivity (1.4 Q.m), as shown in Fig. 7a and 8. These velocity and resistivity values were extracted from an area adjacent to the CNE03 pockmark (see section 3.1), and therefore, represent the $V_p$ and resistivity of the background sediments, as well as in good agreement with the values derived from the macro-scale background core measurements (section 4.1, Figs. 2 and 3). Thus, the approach applied here maintains consistency between remotely-sensed data used for model calibration (background) and that from the anomaly (CNE03), supported by our core analysis. For a hydrate-free scenario, a porosity of ~0.38 (Fig. 8) is required to explain the anomalous $V_p$ and resistivity values observed within the CNE03 pipe-like structure, between ~200–280 mbsf (Fig. 2). Thus, a decrease in porosity due to an increase in the effective stress is insufficient to explain the observed $V_p$ and resistivity anomalies, because ~0.38 porosity is unrealistic for the Nyegga pockmark field, as documented by Hustoft et al. (2009).

We used a critical porosity $\phi_c$ of 0.6, which is consistent with the value commonly used for clay-rich sediments (e.g., Ellis, 2008), and the average porosity measured in our sediment cores (Fig. 3b). Clay minerals have generally low aspect ratio (e.g., Hornby et al., 1994; Jakobsen et al., 2000). Although other minerals such as quartz might have higher aspect ratios, we used a single aspect ratio for simplicity to reduce the degrees of freedom of the model. This single aspect ratio acts as an effective (or average) aspect ratio, as suggested by Han et al.
We found that for an average porosity of 0.6, a combination of 0.2 aspect ratio, \( c \) of 0.6, and the physical properties of clay, quartz, and brine (Table 3), the two-phase model was able to fit the background sediment VP and CSEM resistivity averaged values of 1.7 km/s and 1.4 m, respectively (Fig. 8a and b). The VP and resistivity data obtained from the background core analysis (Fig. 3b) also show good agreement with the calibrated model (Fig. 8a and b), thus, validating our two-phase model calibration procedure.

Next, we used the parameters obtained from the model calibration to generate a three-phase model (where hydrates are included) by running the two-phase SCA/DEM step twice, as illustrated in Fig. 7b. Using the three-phase combined SCA/DEM method and hydrate properties taken from Goldberg et al. (2000); Best et al. (2013), we generated a three-phase model that describes the elastic and electrical response for the entire range of hydrate saturation (Fig. 9a). As a general trend, hydrate content increases with porosity, controlling the joint elastic-electrical properties of a pore-filling hydrate reservoir. At constant hydrate saturation, \( V_P \) and electrical resistivity decrease with increasing porosity, as expected (i.e., for a given hydrate content the brine content increases with porosity, leading to decrease in bulk resistivity and sediment stiffness).

The generated three-phase model can be used as a template onto which the CSEM and seismic derived resistivities and velocities from points of interest can be co-rendered to estimate the hydrate content.

---

**Table 3**

Physical properties of the constituents used in the SCA/DEM effective medium models.

<table>
<thead>
<tr>
<th>Constituent</th>
<th>( K ) (GPa)</th>
<th>( \mu ) (GPa)</th>
<th>( \rho ) (( \Omega )m)</th>
<th>( d ) (g cm(^{-3}))</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quartz</td>
<td>36.6</td>
<td>45</td>
<td>10(^5)</td>
<td>2.65</td>
<td>Mavko et al. (1998); Han et al. (2011a)</td>
</tr>
<tr>
<td>Clay</td>
<td>20.9</td>
<td>6.85</td>
<td>33</td>
<td>2.58</td>
<td>Mavko et al. (1998); Han et al. (2011a)</td>
</tr>
<tr>
<td>CQ mix(^a)</td>
<td>26.7</td>
<td>15.63</td>
<td>95</td>
<td>2.61</td>
<td>Computed</td>
</tr>
<tr>
<td>Brine</td>
<td>2.29</td>
<td>0</td>
<td>0.185</td>
<td>1.025</td>
<td>Telford et al. (1990), and Computed ( \rho )</td>
</tr>
<tr>
<td>Hydrate</td>
<td>7.9</td>
<td>3.3</td>
<td>200</td>
<td>0.925</td>
<td>Goldberg et al. (2000); Best et al. (2013)</td>
</tr>
</tbody>
</table>

\(^a\)\( K \) = Bulk modulus, \( \mu \) = Shear modulus.

\(^b\)\( \rho \) = Resistivity, \( d \) = Density.

\(^*\) Clay + Quartz (CQ) mix, containing 55% clay and 45% quartz.
We used velocities $V_{P1}$, $V_{P2}$, $V_{P3}$ and constant resistivity $\sim 3 \, \Omega \cdot m$ (Fig. 2), to produce three sets of $V_P$–resistivity pairs in order to estimate the hydrate saturation within the three intervals shown in Fig. 2a. For each interval, the $V_P$ and resistivity are similar. Then, in the absence of in-situ porosity data, we can randomly assign porosity values between 0.55 and 0.65 (in accordance with the fluctuating regional porosity (Hustoft et al., 2009), and the porosity derived from the CNE03 core measurement) to each $V_P$–resistivity pair in order to evaluate what hydrate saturation estimates correspond to these porosity ranges.

Fig. 9 shows the three sets of $V_P$–resistivity pairs co-rendered with our joint elastic-electrical SCA/DEM model for hydrate estimation at the porosities of interest. In the upper depth interval, we infer a hydrate saturation of $\sim 20$–$34\%$. In the middle depth interval, the hydrate saturation locally increases up to $\sim 40\%$ (Fig. 9b). In the deeper interval, the inferred hydrate saturation range is $\sim 30$–$48\%$. For the entire porosity range (0.55–0.65) and all depth intervals, the hydrate saturation varies between $\sim 20$ and $48\%$. Using the weighted contribution of each depth interval ($V_P$ dependent) to this CSEM–seismic combined prediction of hydrate saturation, we infer that for porosities 0.55, 0.6 and 0.65, the average of gas hydrate contents are $\sim 25$, $30$ and $40\%$, respectively, within CNE03 between 80 and 280 mbsf. For the regional average porosity of 0.6, the gas hydrate content is $\sim 23$, 33 and 37\% for depth intervals 80–180, 180–200 and 200–280 mbsf, respectively (Fig. 9b).

5.2.1. Sensitivity analysis

A sensitivity analysis was performed using CQ mixes that contain (a) 65\% clay and 35\% quartz, and (b) 45\% clay and 55\% quartz, thus, $\pm 10\%$ clay content then the content obtained from the XRD analysis (section 4.4, Table 2). The analysis indicates subtle changes ($< 2\%$ in gas hydrate saturation (Appendix B, Fig. A1), where lower clay content (higher quartz content) leads to a moderate decrease in gas hydrate content and vice versa. This is due to the higher values of the physical parameters (moduli, resistivity, density) of quartz in comparison to those of clay (Table 3). However, there is no evidence to suggest the sediment composition is different from what we obtained from the XRD measurements performed on CNE03 core samples, which we used for the SCA/DEM modelling.

6. Discussion

A detailed characterisation of the study site lithology is essential to achieve a well constrained and accurate quantification of a gas hydrate deposit. Our results indicate that the background and CNE03 sediments exhibit significant differences in all the three scales (macro, meso, micro) analysed. Here, we highlight the distinctive lithology of the CNE03 pockmark and discuss the limitations and merits of the joint elastic-electrical SCA/DEM modelling scheme for gas hydrate quantification.

6.1. CNE03 lithology: further insights from core analysis

The background sediments demonstrate subtle variations in foraminiferal content and ice-rafted debris, with moderate to extensive bioturbation throughout. These sediments present consistent colour, with gradually increasing resistivity down-core, correlated with hemipelagic silts (Fig. 3a). There is no evidence of deposition of mass wasting events, and stratification is only visible through horizons of intensely bioturbated material. Furthermore, this background core exhibits a continuous record of open marine sedimentation, unaffected by hydrothermal or chemosynthetic processes.

In contrast, the sediments obtained from the CNE03 pockmark show intact shell-rich horizons, cavities, and potent sulfide odour. This odour suggests anaerobic oxidation of methane as well as the presence of sulfide-oxidising bacteria that are hosted by the Isorropodon nyeggaensis sp. bivalves and consume methane as part of their metabolism (e.g., Distel, 1998). Thus, these features are all indicative of hydrate formation processes and dissociation upon core recovery. The properties of the CNE03 core are consistent with cores collected from pockmarks elsewhere in the North Atlantic (e.g., Paul et al., 2006; Panieri et al., 2014). The shell-rich horizons (Fig. 4, Table 1) detected in the CN2, and CN4 units of CNE03 (Fig. 3c) are interspersed with cavities across the core. Radiocarbon analysis to compare these shells and benthic foraminifera to those obtained from the Storegga Slide (e.g., Evans et al., 1996; Hjelstuen et al., 2005; Micallef et al., 2007), may elucidate whether a widespread methane release in Nyegga and the Storegga Slide occurred simultaneously or sequentially.

Fragments of carbonate nodules were observed in the vicinity of these shell-rich horizons, consistent with the recovery of methane-derived authigenic carbonates from nearby pockmarks (Hovland et al., 2005; Mazzini et al., 2006; Ivanov et al., 2010). Methane release occurs predominantly during deglaciation and for a period after deglaciation (Crémieure et al., 2016a). Therefore, authigenic carbonates commonly precipitate in Holocene sediments near the seafloor as a result of methane oxidation by microbial communities (e.g., Hustoft et al., 2007; Mazzini et al., 2006; Petersen et al., 2010; Riboulot et al., 2016; Crémieure et al., 2016b). Thus, we postulate that authigenic carbonates may contribute to the higher resistivity observed near the seafloor.
(< 10 mbsf) at CNE03, whereas the resistivity and V_p anomalies detected at depth are most likely due to the presence of hydrate rather than authigenic carbonate. However, our core data does not extend deep enough to confirm that. We hypothesise that both the shell-rich horizons and authigenic carbonates were formed during periodic venting of methane from this pockmark, consistent with previous findings from the Nyegga pockmark field (Paull et al., 2008; Vaular et al., 2010).

Overall, we observe very little difference between the elastic and electrical properties of the background samples and the CNE03 samples (Fig. 3b). Due to the meso-scale measurements confining pressure and the nature of contact between the electrodes and samples (section 3.2.2), the V_p and resistivity values are overestimated in comparison to the macro-scale measurements, thus limiting their ability to provide evidence of hydrate dissociation in the CNE03 core. However, we postulate that unpressurized recovery of this core has led to hydrate dissociation (Fig. 1); and consequently, the release of gas via porous flow due to the high porosity of the sediment (~0.6), leaving mainly water-filled regions within the CNE03 cores (Fig. 3).

6.2. SCA/DEM modelling for hydrates

In addition to being sensitive to microstructural details, rock physics models are also sensitive to the petrophysical properties of the sediments, making them prone to non-uniqueness. The joint elastic-electrical approach contributes in mitigating this non-uniqueness. To constrain further the rock physics models, we made use of data from a comprehensive analysis of the retrieved sediment cores. The information from core data assists in constraining important controls on elastic and electrical properties such as the mineralogy and porosity. These steps helped to reduce the non-uniqueness in the models significantly.

The aspect ratio used in the modelling is not very well-constrained, as it is difficult to estimate accurate aspect ratios, even from core data, due to the variety of aspect ratios that can be found in sediments. Clay minerals have low aspect ratios while minerals such as quartz and calcite are normally assigned with aspect ratios equal to unity (e.g., Hornby et al., 1994; Mavko et al., 1998; Jakobsen et al., 2000). Han et al. (2011a) suggested calculating an effective aspect ratio of each inclusion by averaging individual aspect ratios weighted by their volume fractions as a way of mitigating this complexity. Although we
arrived at the aspect ratio of 0.2 by fitting a two-phase model to the background response, this value is in agreement with that derived from the averaging approach suggested by Han et al. (2011a). If we assume the pore space (brine) is of the same low aspect ratio as clay, and both of them equal to 1/40 (e.g., Jakobsen et al., 2000), then assigning an aspect ratio of 1 to quartz and averaging the aspect ratios by their volume fractions gives an aspect ratio of about 0.2.

Clay-rich sediments are anisotropic when the clay minerals are preferentially aligned in a given direction. However, we have used isotropic formulations of the effective medium theories because a comparison between CSEM isotropic and anisotropic inversions suggested that anisotropy at CEN03 is very subtle, and the isotropic models were able to fit the data adequately (Attias et al., 2016). Therefore, accounting for anisotropy without the information/data to constrain it would lead to more uncertainties from additional free parameters (e.g., anisotropic mineral moduli, orientation distribution functions). Consequently, we applied an isotropic approach, where the low aspect ratio clay minerals are randomly aligned.

6.3. Modelling limitations

The main limitation of our SCA/DEM joint elastic-electrical modelling approach is that it assumes a pore-filling morphology. We chose to use a pore-filling morphology partly based on the evidence mentioned above (sections 1, and 5.1), and partly due to modelling considerations. The modelling considerations result from model parameterization, aiming to minimize the number of free (unconstrained) parameters as much as possible to reduce uncertainties. The trade-off is between accounting ideally for the geologic complexity via formulating a joint modelling approach, and a more simplistic approach that only accounts for some of the geological complexity yet remains predictive. The pore-filling morphology provides a balance between subsurface geological complexity and model reliability.

Another limitation is related to the difference in resolutions of the seismic velocity and CSEM remote sensing data that we used in our SCA/DEM modelling scheme. Attias et al. (2018) imaged the resistivity structure of the CNE03 pockmark in high-resolution using 2.5-D CSEM inversions of a towed-receiver data individually and jointly with seafloor receivers data. Their results were supported by a linearized sensitivity analysis to the inversion models by evaluating the model Jacobian matrix J (e.g., Farquharson and Oldenburg, 1996; Key, 2016). By co-rendering the inversion models with the J contours, Attias et al. (2018) demonstrated the high-sensitivity of the model to the entire pipe-structure at CNE03 (Plaza-Faverola et al., 2010). Seismic reflection sections and velocity model of the CNE03 pipe-structure agrees well with our CSEM inversion models, which increase the level of our confidence in the joint electrical and elastic properties. Using the best fitting model, we explored the possible physical properties (porosity and saturation) via the joint elastic-electrical modelling approach.

The joint elastic-electrical effective medium modelling scheme presented here provides a rigorous method to quantify the saturation of gas hydrate in a pore-filling morphology, as it considers microstructural information. Although this modelling approach might not be ideal for the CNE03 pockmark, the concepts and workflow described above can be applied to quantify gas hydrate reservoirs in a purely pore-filling morphology with fine-grained muddy clay sediment, as documented in studies from South China Sea (e.g., Zhang et al., 2007; Zhong et al., 2017; Liu et al., 2019) and eastern Nankai Trough, Japan (Yoned a et al., 2017).

6.4. CNE03: Gas hydrate quantification

Previous seismic velocity (using reflection time tomography) and CSEM resistivity (using Archie’s) analysis to predict the hydrate content within CNE03 inferred saturations of 14–27% of total volume, which is equal to 23–45% of pore volume (Plaza-Faverola et al., 2010), and ~38% of pore volume (Attias et al., 2016), respectively. Here, our joint elastic-electrical SCA/DEM approach yields an inferred hydrate saturation of ~23, 33 and 37% for the three (depth dependent) Vp intervals, as described in section 5.2. Thus, comparable with both the seismic and CSEM individual predictions, but provides a more detailed assessment of hydrate saturation via rigorous rock physics framework.

Comparisons of coincident electrical and elastic datasets with the joint elastic-electrical SCA/DEM models enabled us to determine the depth-dependent lower and upper bounds of the gas hydrate saturation in the CNE03 pipe-like structure (Fig. 9). The Vp and resistivity anomalies observed within the CNE03 pipe-like structure above the BGHSZ implied that hydrates might be localized rather than porosity decrease (effective stress increase) with depth. Otherwise, a porosity of ~0.38 would be required to account for these anomalies (Fig. 8), which does not seem realistic for the Nyegga pockmark field (section 5.2). Additionally, if the porosity of the FE23 structure is only ~0.38, we infer that the amount of free gas within the GHSZ of CNE03 is significant. Consequently, we chose to neglect the free gas from our modelling of gas hydrate saturation (section 5.2), thus avoid introducing unknown parameters that may increase the model uncertainties and most likely bias the results.

7. Summary and conclusions

This paper offers both qualitative and quantitative analysis of the CNE03 gas hydrate pipe-like structure, in the Nyegga region, Offshore Norway. Sediment cores were characterised at macro-, meso- and micro-scale for lithological and petrophysical properties, providing important constraints on model inputs. A rock physics framework that links the elastic and electrical properties of an effective medium was applied to quantify gas hydrate saturation from coincident marine CSEM and seismic data. The self-consistent approximation and differential effective medium theories were combined to generate a fully connected three-phase model, with the steps chosen to achieve an idealised representation of pore-filling hydrate morphology.
Based on this work, we conclude the following:

1. The sediment core analysis provides evidence for the formation and dissociation of gas hydrate within the CNE03 pipe-like structure, as inferred from the recovery of hydrate and chemosynthetic bivalves.

2. The background VP and resistivity values obtained from the macroscale measurements are comparable with the seismic velocity and CSEM resistivity remote sensing data derived from the area adjacent to the CNE03 pockmark. However, the macro-scale measurements were derived from 6 to 8 m sediment cores; and therefore, may not ideally represent the remotely-sensed seismic velocity and CSEM resistivity obtained from the deeper layers of the area adjacent to the CNE03 pockmark.

3. Comparison of the collocated CSEM and seismic datasets with the joint elastic-electrical SCA/DEM model indicates that the gas hydrate saturation within CNE03 ranges from ~20% to ~48%, at a porosity range of 0.55–0.65, between depths of 80 and 280 mbsf.

4. For porosities 0.55, 0.6, and 0.65, the hydrate saturation varies between ~20–34%, ~23–37%, and ~30–48%, whereas the weighted means are ~25, 30 and 40%, respectively.

5. The hydrate saturation at CNE03 gradually increases with depth, whereas the highest hydrate saturation is near the base of the gas hydrate stability zone.

6. Our elastic-electrical combined analysis predicts hydrate saturation of ~23–37%, consistent with the elastic (23–45%) and electrical (~38%) individual predictions, previously conducted at CNE03.

7. The coupling of seismic and CSEM data using a joint elastic-electrical effective medium model is a more rigorous framework for the estimation of hydrate saturation, particularly when model parameters are well-constrained.

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Appendix A

The SCA equation for the elastic moduli and electrical conductivity for ellipsoidal inclusions are given by Mavko et al. (1998):

\[
\sum_{j=1}^{m} x_j (K_j - K_{SC}) P_j = 0,
\]

\[
\sum_{j=1}^{m} x_j (\mu_j - \mu_{SC}) Q_j = 0,
\]

and

\[
\sum_{j=1}^{m} x_j (\sigma_j - \sigma_{SC}) C_j = 0,
\]

Where \(j\) denotes the \(j\)th material, with volume fraction \(x\), bulk modulus \(K\), shear modulus \(\mu\), and electrical conductivity \(\sigma\). The coefficients \(P\), \(Q\) and \(C\) are geometric factors for ellipsoidal inclusions of arbitrary aspect ratios in a background medium with self-consistent effective bulk and shear modulus, and electrical conductivity of \(K_{SC}\), \(\mu_{SC}\), and \(\sigma_{SC}\), respectively.

The general DEM expressions for the elastic moduli and electrical conductivity are given by Mavko et al. (1998):

\[
dK_{DEM}(x_j) = \frac{(K_j - K_{SC}) P_j}{1 - x_j} dx_j,
\]

\[
d\mu_{DEM}(x_j) = \frac{(\mu_j - \mu_{SC}) Q_j}{1 - x_j} dx_j,
\]

and

\[
d\sigma_{DEM}(x_j) = \frac{C_j (x_j - \sigma_{SC})}{1 - x_j} dx_j,
\]

Where the terms are as described for the SCA equations above.

Appendix B

Sensitivity analysis using CQ mixes that contain (a) 65% clay and 35% quartz, and (b) 45% clay and 55% quartz, thus, ± 10% clay content then the content obtained from the XRD analysis. This analysis indicates subtle changes (< 2%) in gas hydrate saturation, where lower clay content (higher quartz content) leads to a moderate decrease in gas hydrate content and vice versa (Fig. A1). This is due to the higher values of the physical parameters (moduli, resistivity, density) of quartz in comparison to those of clay.
Fig. A1. Model sensitivity analysis. Comparison of the joint elastic-electrical properties obtained from the SCA/DEM model with CSEM and seismic remote sensing data, with three different CQ mixes. (a) The CQ mix contains 65% clay and 35% quartz. (b) The CQ mix contains 55% clay and 45% quartz, corresponding to the values derived from the XRD analysis (Table 2) and used in the manuscript (Fig. 9). (c) The CQ mix contains 45% clay and 55% quartz. White circles denote depth interval 1: 80–180 mbsf, $V_p \approx 1.75$ km/s; White-black gradient circles denote depth interval 2: 180–200 mbsf, $V_p \approx 1.83$ km/s; Black circles denote depth interval 3: 200–280 mbsf, $V_p \approx 1.90$ km/s. The resistivity for the three depth intervals is $\sim 3 \, \Omega m$ (see section 3.1). The dashed contour represents 35% of gas hydrate saturation. Note the subtle decrease in the gas hydrate saturation as indicated by superimposing the remotely sensed data (best visible in Figure insets). This decrease results from increasing the quartz content in the CQ mix.


